

Letters

Intrinsic viscosity and friction coefficient of polymers in solution*

It has been known for a long time that a polymer in solution cannot be represented by a hard sphere due to the finite permeability of the coil which enables the solvent to flow through as well as around the coil. In this Letter we summarize an *a priori* calculation of the flow of a solvent through a polymer coil and of the two most important frictional properties of macromolecules in solution: the intrinsic viscosity and the translational friction coefficient. Detailed derivations and discussions of the results will be published elsewhere^{1,2}.

The stationary flow of a fluid through and around a permeable polymer has to be solved from the Debye-Brinkman equation:

$$-\vec{\nabla}P + \eta_0 \Delta \vec{V} - \frac{\eta_0}{k} (\vec{V} - \vec{U}) = 0 \quad (1)$$

In equation (1) P and \vec{V} denote the average local pressure and velocity of the solvent, \vec{U} the local velocity of the polymeric material, η_0 the viscosity of the pure solvent and k the local permeability. If the fluid is incompressible, this is expressed by:

$$\text{div } \vec{V} = 0 \quad (2)$$

For a realistic model of the polymer the permeability has a radial dependence

Table 1

α	$\Phi(\alpha)$	$\Psi(\alpha)$
0	0.332	0.443
1	0.321	0.359
2	0.311	0.303
3	0.301	0.263
4	0.292	0.233
5	0.284	0.209
6	0.277	0.190
7	0.270	0.175
8	0.263	0.162
9	0.257	0.151
10	0.251	0.141
11	0.246	0.133
12	0.241	0.125
13	0.236	0.119
14	0.231	0.113
15	0.227	0.108
16	0.223	0.103
17	0.219	0.099

* Based on a paper presented at the conference, Theoretical methods in Polymer Physics, Leeds, July 1976

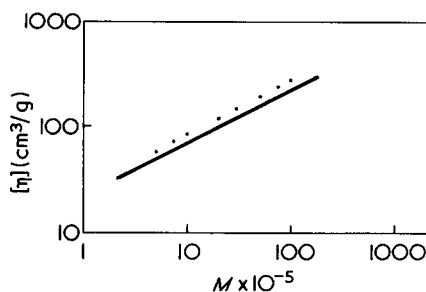


Figure 1 Predicted and experimental values of $[\eta]$ for system A. ●, values calculated from equation (4); —, empirical curve

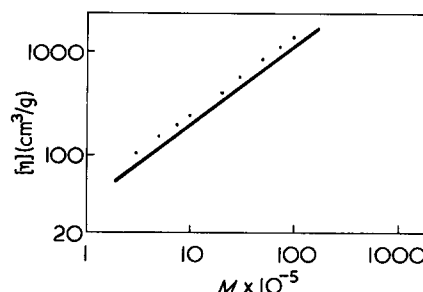


Figure 2 Predicted and experimental values of $[\eta]$ for system B

which can be shown to be given by an expression of the form:

$$k(r) = K \exp(Qr^2) \quad (3)$$

where r is the distance to the centre of gravity of the coil and where Q (which is directly related to the radius of gyration) and K are positive constants. Their values, which depend on the polymer (including its molecular weight), on the solvent and on temperature can be derived from light scattering measurements and from sedimentation experiments at finite concentration (which give the permeability as a function of concentration).

By solving equations (1), (2) and (3) under the appropriate boundary conditions one finds for the intrinsic viscosity:

$$[\eta] = \frac{4}{3} \pi m^{-1} K^{-1} Q^{-5/2} \Phi(K^{-1} Q^{-1}) \quad (4)$$

and for the translational friction coefficient (frictional force on the coil per unit of relative velocity between solvent and coil):

$$f = 4\pi \eta_0 K^{-1} Q^{-3/2} \Psi(K^{-1}) \quad (5)$$

The mass of a polymer is denoted by m . The dimensionless functions Φ and Ψ of the dimensionless parameter $\alpha \equiv K^{-1} Q^{-1}$ are tabulated in Table 1. For realistic cases values of α appear to lie around 10.

These results enable us to predict the value of $[\eta]$ and f for polymer-solvent systems for which data about the radius of gyration and about permeability as a function of concentration are available. Systems for which this is the case are: (system A) poly(α -methylstyrene) in cyclohexane at 35.5°C (a system at θ -condition); (system B) poly(α -methylstyrene) in toluene at 25°C (an approximately athermal system).

The predicted and observed values of intrinsic viscosity and friction coefficient for these two systems are compared in Figures 1-4, in which the dots are the predicted values whereas the solid lines represent the empirical values. Agreement between theory and experiment is satisfactory, in particular in view of the fact that not a single parameter has been adjusted.

It should be mentioned, however,

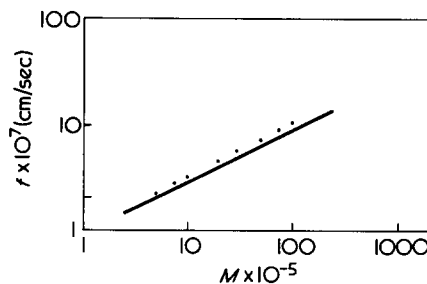


Figure 3 Predicted and experimental values of f for system A. ●, values calculated from equation (5); —, empirical curve

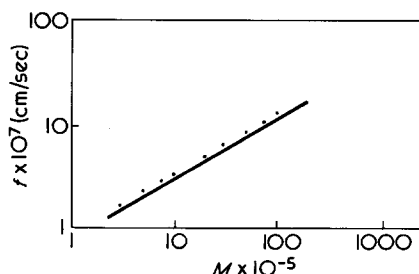


Figure 4 Predicted and experimental values of f for system B

that the results are quite sensitive for the value of K and that the permeability curves, from which K is derived, are not at all the same for the two systems considered^{3,4}. When $[\eta]$ and f for system B are calculated on using K values derived from the permeability curve pertaining to system A the results

are wrong by a factor of about 3.

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Proton spin-lattice relaxation in poly(vinyl acetate) in solution

In a recent paper¹, it was shown that proton-lattice relaxation measurements of polymers in solution were able to discriminate between various models for polymer motion which were equally successful in interpreting ¹³C relaxation data². It was found that the conformational jump dynamic model³ of polymer motion combined with overall molecular tumbling⁴ was the only model (of those considered) which explained all the experimental data consistently over a wide temperature range. The advantage of the ¹H relaxation measurements over ¹³C measurements lay in their ability to sense spectral density functions at both low frequencies of the order of ¹H-¹H chemical shifts and high frequencies of the order of the instrumental frequency. It is desirable to test the validity of the conformational jump model further by making measurements at different operating frequencies. In this communication we therefore report proton relaxation data at 100 MHz for a solution of poly(vinyl acetate) in toluene-*d*₈ of concentration 134 mg/ml. Relaxation data at 300 MHz for this system has been reported earlier^{1,5}.

Two correlation times, τ_D and τ_0 , determine the correlation function for the conformational jump model^{3,4}. τ_D characterizes the local jumps of a chain on a tetrahedral lattice³, and τ_0 characterizes the overall molecular tumbling⁴. Using procedures outlined previously¹, it is possible to obtain both correlation times, subject to certain restrictions, from the results of several types of relaxation experiments. These are¹: (a) effective relaxation times of methine (A) and methylene (X) protons in the normal non-selective inversion recovery technique ($\pi-\tau-\pi/2$), denoted T_{1A}^{eff} and T_{1X}^{eff} , (b) relaxation times for the A protons when X is decoupled (T_{AA}) and *vice versa* (T_{XX}); (c) nuclear Overhauser enhancements of each type of proton when the other is saturated, η_A and η_X .

From the experimental data at 300 MHz, the values of τ_D and τ_D/τ_0 given in the second and third columns of *Table 1* have been derived⁵. At certain temperatures, a considerable range of values of τ_D and τ_0 fit the data satisfactorily. The remaining columns in *Table 1* compare the experimental parameters for the methine nucleus at 100 MHz with the corresponding values calculated¹ using these correlation times. Unfortunately at the lower frequency the overlap of methyl and methylene resonances is too severe to allow accurate measurement of the methylene relaxation times. The agreement between experimental and calculated values is quite good, allowing for respective uncertainties of the order of 10% and 30%. The two-parameter conformational jump model thus satisfies the frequency variation of relaxation times.

The temperature variations of τ_D and τ_0 for this sample parallel those for a less concentrated sample¹ of 17 mg/ml. τ_0 obeys an Arrhenius equation (within experimental error) with an activation energy of 12 ± 2 kJ/mol, while τ_D appears to undergo a rapid transition from values less than τ_0 to values greater than τ_0 . At temperatures greater than about 10°C, the auto-

correlation function decay is dominated by segmental motion, but at lower temperatures, the decay is dominated by overall tumbling. The values of τ_D at higher temperatures are essentially the same as those for the lower concentration¹, consistent with a local short-range reorientation process. The values of τ_0 are however significantly larger than those for the lower concentration, as expected for a large-scale motion likely to be more responsive to bulk solution viscosity.

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Table 1 Relaxation data for poly(vinyl acetate) in toluene-*d*₈, concentration 134 mg/ml. The correlation times are those obtained from data at 300 MHz^{1,5}. The relaxation times predicted at 100 MHz for these correlation times are compared with the experimental values

T (°C)	Calculated			Experimental				
	τ_D (psec)	τ_D/τ_0	T_{1A}^{eff} (msec)	T_{AA} (msec)	η_A	T_{1A}^{eff} (msec)	T_{AA} (msec)	η_A
84	0.061	0.06	400	440	0.29	360	380	—
48	0.154	0.1	275	300	0.23	240	260	0.2
16	{ 1.33	0.3	170	170	-0.05	190	190	0.0
	{ 1.0	0.4	170	180	0.1			
5	{ 4.22	1.0	160	150	-0.13	180	170	-0.1
	{ 2.56	10.0	130	130	-0.06			
-23	{ 56.2	10.0	160	120	-0.45	180	130	-0.55
	{ 394.0	100.0	150	120	-0.35			
-40	700	100.0	200	100	-0.66	240	70	-0.75